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SATELLITE & MESOMETEOROLOGY RESEARCH PROJECT

Department of the Geophysical Sciences
The University of Chicago

ON THE DETERMINATION OF EXCHANGE COEFFICIENTS: PART II ROTATING AND NONROTATING CONVECTIVE CURRENTS

by Rodger A. Brown

SMRP Research Paper #54

January

1966

The research reported in this paper has been partly supported by the Air Force Cambridge Research Laboratories of the Office of Aerospace Research, USAF, Bedford, Mass., under Contract No. AF 19(628)4807 and partly by the National Severe Storms Laboratory, U. S. Weather Bureau, under grant Cwb WBG - 41.

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10. Conclusions

Through the study of the wind speed of the Palm Sunday tornadoes, five important characteristics of tornado circulation were found. They are: (1) a tornado circulation is characterized by a nearly circular core surrounded by an irrotational vortex, (2) there are several spots of strong suction along the edge of the core; (3) the core changes its shape and diameter, (4) the rotational rate of the core increases as the mean core diameter decreases, and (5) a tornado cyclone surrounding a tornado is almost axially symetric as far as the pressure field is concerned, but the front and the rear sides are dominated by convergence and circulation, respectively

This study has shown that it is highly important to perform aerial surveys of the damage paths of future tornadoes. Such surveys should investigate the damage patterns by undisturbed tornado vortices, such as could be formed over open fields.



the loop tops and the path of the tornado center. The phase angles were computed from the positions of the recess of perpendiculars dropped from each loop top to the path of the tornado center.

Of interest is the change in the stippled area obtained by smoothly connecting the suction spots. The number of suction spots varied between 4 and 5 while their vactors changed considerably from time to time. It should be noted that the rotational period decreased as the mean diameter of the stippled area shrunk as the storm moved eastward. This would imply that (1) the shrinkage of the stippled area increased the rotational rate, keeping probably the angular momentum constant and that (2) the stippled area represents the central core of the tornado, which kept deforming rather rapidly.

The mean tangential speeds of the suction spots when the tornado center was at locations 1 through 7 are 110, 114, 111, 118, 118, 111, and 104 mph, respectively. By adding 62.5 mph to these values, we obtain the maximum ground speeds of 178, 176, 173, 180, 180, 173, and 166 mph, respectively.

These tangential speeds are very similar to those of funnel rotation obtained by Fujita (1959) using motion pictures of the Fargo tornadoes of June 20, 1957. The tangential speeds of seven pendants appearing at the base of a sheared-off funnel just above the ground were 112 (90), 112 (60), 93 (30), 100 (60), 111 (110), 100 (100), and 102 fnph (90), respectively. The numbers in parenthesis are the distance of the pendants from the funnel center.

From these results, it will be reasonable to assume that these suction spots rotate around the tornado center with approximately the rotational rate of the funnel.

/9. Conclusions

%. Computation of the Rotational Rate of Suction Spots

It has been shown in the previous section that n, the ratio of tangential and translational speeds of a suction spot can be obtained by measuring W, the relative loop width on an aerial photograph. Under the fair assumption that a suction spot rotates around the tornado center, we obtain the tangential speed of a suction spot as a product of n times $U_{10}R$, the translational speed of the tornado.

The speed of a fast-moving tornado seems to be rather constant, It is probably because tornadoes tend to move, on the average, with the speed of the parent thunderstorm. In Fig. 14 diagram of a family of six tornadoes in series time space which traveled from Indiana to Ohio as shown in Fig. 2, Chapter II. This family of tornadoes left a damage path in almost & straight line 274 miles long during a period of 4 hr 23 min. From the slope of a diagonal line through the black dots in the figure $\mathcal{O}_{\mathsf{ToR}}$ was estimated to be 62.5 mph.

In order to apply the technique of cycloidal curve analysis presented in the previous section, a picture of a group of suction marks taken along the path of the above-mentioned tornado family was investigated in detail. An aerial photograph taken and rectified by the author is shown in Fig. 15. The horizontal scale and the estimated path of the tornado center are superimposed in the photograph.

Traced suction marks appearing in Fig. 16 permit us to compute the relative loop width, w, which can be converted into both and S by using two curves in Fig. 13. In this case, we computed S to represent the distance of the loop shift. Two persistent suction spots, identified with letters a and e, were followed during their one to the rotation periods, thus determining the expected locations of their periodic appearances of the loops.

The open circles with numbers 1 through 7 are the estimated positions of the tornado center after the suction marks completed each revolution around the center. The distance of travel during each revolution can be converted into the rotational period by assuming $U_{\text{Tor}} = 62.5 \text{ mph}$. The periods in seconds given in the figure are the rotational periods thus obtained.

The figure also shows the positions of the suction spots when the tornado center was at the locations 1 through 7. In determining the positions of these suction spots, the radius vectors were obtained by measuring the distance between

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| Table I. | Relative loop width 11) | |
|----------|---|-----------|
| 0 | Relative loop width, W, in increments 2 m, the ratio of tangential to to reads. | fool, |
| sp | reeds. | - Comment |

Table II. Relative loop width, Us in increments of 0.01, vo the relative loop shift, 5.

Put W at had y column and retype table with

0.0 0.00 0.01 0.02 0.03 0.04 0.05 atc.

0.1

0.2

0.3

0.4

0,5

Table I Relative loop width, vs.

28

| W | 0.0 | 0.40 | 0,2 | 0.3 | 0.6 | 0.50 | 0.6 | 0.7 | 0.8 | 0.9 | |
|-------|------|------|------|------|------|------|-------|------|-------|-------|--|
| 0.0 D | 1.00 | 1.29 | 1.54 | 1.85 | 2.24 | 2.78 | 3.58 | 4.89 | 7.52 | 15.38 | |
| 0.07 | 1.05 | 1.31 | 1.57 | 1.88 | 2.29 | 2.84 | 3.68 | 5.08 | 7.94 | 17.13 | |
| 0.02 | 1.08 | 1.33 | 1.60 | 1.92 | 2.33 | 2.91 | 3.78 | 5.21 | 8.40 | 19.31 | |
| 0.03 | 1.11 | 1.36 | 1.63 | 1.95 | 2.38 | 2.98 | 3.90 | 5.48 | 8.91 | 22.12 | |
| 0.04 | 1.14 | 1.38 | 1.66 | 1.99 | 2.43 | 3.06 | 4.02 | 5.70 | 9.49 | 25.86 | |
| 0.05 | 1.16 | 1.41 | 1.69 | 2.03 | 2.48 | 3.13 | -4-14 | 5.95 | 10.14 | 31.09 | |
| 0.06 | 1.19 | 1.44 | 1.72 | 2.01 | 2.54 | 3.21 | 4.27 | 6.21 | 10.89 | 38.95 | |
| 0.07 | 1.21 | 1.46 | 1.75 | 2.11 | 2.60 | 3.30 | 4.42 | 6.49 | 11.76 | *** | |
| 0,08 | 1.24 | 1.49 | 1.78 | 2.15 | 2.65 | 3.39 | 4.57 | 6.81 | 12.76 | *** | |
| 0.09 | 1.26 | 1.51 | 1.81 | 2.19 | 2.71 | 3.48 | 4.12 | 7.15 | 13.95 | *** | |

** no values computed because of too large on

loop width vs. Relative Relative 0.9 0.0 0.1 0,2 0.3 0.4 0.7 0,8 0.5 0.6 0.64 0.42 0.21 0.88 1.70 1.40 1.13 3.14 2.44 0.00 0.85 0.18 0.62 0.40 2.00 1.37 1.10 1.67 2.97 2.40 0.01 0.83 0.38 0.17 2.90 0.60 1.97 1.64 1.35 1.08 2.36 0.02 1.60 1.32 1.05 2.83 0.14 1.94 0.81 0.58 0.35 0.03 2.31 1.30 1,90 0.55 2.76 1.57 1.02 0.04 2,27 0.78 0.33 0.12 1.87 0.52 1.26 0.10 0.31 0.05 1.5K 0.76 1.00 2.20 2.23 0.08 1.84 2.64 2.18 1.24 0.73 0.06 0.98 0,51 0,29 1.52 2,15 1,2/ 0.95 1.48 0.27 0.06 1.49 0.71 2.59 1.80 0.07 2.12 1.18 0.93 0.69 0.46 0,25 0.08 2,54 1.76 0.04 1.46 0.44 922 0.66 0.02 2.08 1.16 2.49 1.73 1.43 6,90 0.09

Table I. Relative loop width, W, in increments of 0.01, vo. n, the ratio of forgential

| 3J | to | translat | onal p | peeds. | | | | | | |
|----------|------|----------|--------|------------|------|------------------|------|------|-------|-------|
| 15 | 8.08 | 0.01 | 0.02 | etc 0.3 | 0.4 | 0.5 | 0.6 | 0.7 | 0.8 | 0.9 |
| 12 | | | | | | | * | | | |
| 8.60.00 | 1.00 | 1.29 | 1.54 | 1.85 | 2.24 | 2.78 | 3.58 | 4.89 | 7.52 | 15.38 |
| 0.10.01 | 1.05 | 1.31 | 1.57 | 1.88 | 2.29 | 2.84 | 3.68 | 5.08 | 7.94 | 17.13 |
| 0.20.02 | 1.08 | 1.33 | 1.60 | 1.92 | 2.33 | 2.91 | 3.78 | 5.27 | 8.40 | 19.31 |
| 0.3 0.03 | 1.11 | 1.36 | 1.63 | 1.95 | 2.38 | 2.98 | 3.90 | 5.48 | 8.91 | 22.12 |
| 0.04 | 1.14 | 1.38 | 1.66 | 1.99 | 2.43 | 3.06 | 4.02 | 5.70 | 9.49 | 25.86 |
| 0.05 | 1.16 | 1.41 | 1.69 | 2.03 | 2.48 | 3.13 | 4.14 | 5.95 | 10.14 | 31.09 |
| 0.06 | 1.19 | 1.44 | 1.72 | 2.07 | 2.54 | 3.21 | 4.27 | 6.21 | 10.89 | 38.95 |
| 0.07 | 1.21 | 1.46 | 1.75 | 2.11 | 2.60 | 3.30 | 4.42 | 6.49 | 11.76 | *** |
| 0.08 | 1.24 | 1.49 | 1.78 | 2.15 | 2.65 | 3.39 | 4.57 | 6.81 | 12.76 | *** |
| 0.09 | 1.26 | 1.51 | 1.81 | 2.19 | 2.71 | 3.48 | 4.72 | 7.15 | 13.95 | *** |
| · | | | | | * •. | o e ^o | | | | |

^{***} No values computed because of too large n

Table II. Relative loop width, W, vs. relative loop shift, \$

| | 0.00 | 0.01 | 0.02 | 0.03 | etc. 0.4 | 0.5 | 0.6 | 0.7 | 0.8 | 0.9 |
|----------|------|------|------|------|----------|------|------|--------------|------|------|
| 19 | | | | | | | · · | | | |
| 0.00.00 | 3.14 | 2.44 | 2.0 | 1.70 | 1.40 | 1.13 | 0.88 | 0.64 | 0.42 | 0.20 |
| 0.10.01 | 2.97 | 2.40 | 2.00 | 1.67 | 1.37 | 1.10 | 0.85 | 0.62 | 0.40 | 0.18 |
| 0.2 0.02 | 2.90 | 2.36 | 1.97 | 1.64 | 1.35 | 1.08 | 0.83 | 0,60 | 0.38 | 0. |
| 0.3 0.03 | 2.83 | 2.31 | 1.94 | 1.60 | 1.32 | 1.05 | 0.81 | 0.58 | 0.35 | 0.14 |
| 0.04 | 2.76 | 2.27 | 1.90 | 1.57 | 1.39 | 1.02 | 0.78 | 0.55 | 0.33 | 0.12 |
| 0.05 | 2.70 | 2.23 | 1.87 | 1.54 | 1.26 | 1.00 | 0.76 | 0.52 | 0.31 | 0.10 |
| 0.06 | 2.64 | 2.18 | 1.84 | 1.52 | 1.24 | 0.98 | 0.73 | 0.5 D | 0.29 | 0.08 |
| 0.07 | 2.59 | 2.15 | 1.80 | 1.49 | 1.21 | 0.95 | 0.71 | 0.48 | 0.27 | 0.06 |
| 0.08 | 2.54 | 2.12 | 1.76 | 1.46 | 1.18 | 0.93 | 0.69 | 0.46 | 0.25 | 0.04 |
| 0.09 | 2.49 | 2.08 | 1.73 | 1.43 | 1.16 | 0.90 | 0.66 | 0.44 | 0.22 | 0.02 |
| | | | | | | | | | | |

which may be called the "relative loop shift." Since n and w are function of each other, we are able to express s as a function of w only. The right-hand diagram in Fig. 13 presents the relative loop shift as a function of w. It is evident that s decreases from a maximum value of w to zero as the relative loop width increases to 1.0.

More accurate values of n and S are given in Tables I and II in which both quantitues are computed by increasing W at 0.01 intervals. The table permit us to obtain n between 1.00 when W = 0.00 and 38.95 when W = 0.96. Such a range would be sufficient for analytical purposes, since there will be no tornado when n is less than 1.0, and since cycloidal marks are too close to each other if W exceeds about 0.9.



of tangential and translational speeds.

Figure 12 was made by changing from 1.0 to 10. The height of the loop as well as the loop width increases with n, becoming naturally very close to 2 R when exceeds 10.

The loop width is measured as the difference of When the slope changes from plus infinity to minus infinity, which occurs when

$$1 - n \sin 2\pi C = 0$$
or
$$2\pi C = \sin^{-1} \frac{1}{n}.$$
 (3)

The time corresponding to this rotation angle is

$$t = \frac{2\pi c}{\omega} = \frac{2\pi cR}{\sqrt{2}}$$

which is now put into Eq. (1) to obtain

and
$$\chi_2 = \frac{2\pi c R}{n} + \frac{R \sqrt{n^2-1}}{n}$$

and $\chi_2 = \frac{(\pi - 2\pi c)R}{n} - \frac{R \sqrt{n^2-1}}{n}$.

Thus we have

$$W = \chi_1 - \chi_2 = \frac{R}{n} \left\{ 2 \left[n^2 - 1 \right] + 2 \sin^{-1} \frac{1}{n} \right\}$$
 (4)

where W denotes the width of the loop which naturally increases with n.

In order to define a non-dimensional quantity related to the loop width we introduce the ratio of W and 2R, thus

$$\widehat{W} = \widehat{W}/2R = \widehat{n}^{-1} (\widehat{1}\widehat{n^{2}} - \widehat{1} + Sin^{-1}\widehat{n^{-1}})$$
 (5)

which may be called the "relative loop width." It is evident that this quantity varies as the function of only n. It is, therefore, feasible to determine n from measured values of W. Figure 13 presents the variation of was a function of W. This figure permits us to determine n from a suction mark on an aerial photograph and the known value of U.

When a large number of suction marks appear, such as the schematic pattern in Fig. 13, it is very difficult to identify the loops produced by a single suction spot which rotated more than once around the tornado center. In such a case, the distance of the loop shift, s can be estimated from W and R. We shall now define the non-dimensional quantity S as

$$S = \frac{s}{2R} = \frac{2\pi R}{n} / 2R = \frac{\pi}{n}$$
 (6)

be expected.

The size of these spots with strong convergence determined from the width of cycloidal lines is only several to 20 ft, implying that the convergence inside a tornado is concentrated at several spots which rotate around the traveling tornado center. Such spots of concentrated convergence are called the "suction spots," and the ground marks appearing along the loci of suction spots, the "suction marks." Suction marks, if preserved, would represent a group of cycloidal curves; but to strong winds the rear side of a traveling tornado, the marks produced by suction spots while moving the front side are either partially or totally destroyed by those suction spots in the rear side. This is why we frequently see in aerial pictures the rear half of the cycloidal marks more distinctly. Before the end of the tornado wind, however, the rear half will be swept by the remainder of the whir wind. The "drift marks" as indicated in Fig. 11 are the common features produced by debris which is blown off in the direction of the final strong winds.

8. Shape of Cycloidal Marks, and their Loop Width and Loop Shift

If a suction spot is assumed to rotate around the tornado center maintaining a constant radius, the locus of the spot can easily be computed as a function of which are the translational and tangent speeds, and the radius between the spot and the tornado center. Parametric equations of a cycloid with the axis taken along the path of a tornado center are,

$$y = R \sin \omega t$$
and
$$E = Ut + R \cos \omega t$$
(1)

where ω denotes the angular velocity of a suction spot and t, the time measured from the initial t axis crossing to the spot. If $c = \omega t/2 \pi$, the total and fractional rotation number of the suction spots around the tornado center, is substituted in Eq. (1), and differentiated in order to obtain the slope, then

$$\frac{dy}{dx} = \frac{dy}{dt} / \frac{dx}{dt} = \frac{V \cos 2\pi c}{U - V \sin 2\pi c}$$

$$= \frac{n \cos 2\pi c}{1 - n \sin 2\pi c}, \qquad (2)$$

where $n = \sqrt{10}$, the ratio of the tangential and the translational speeds. Eq. (2) indicates that the slope of the cycloidal curve is a function of both n and C without depending upon R, the distance of the suction spot from the rotation center. This means that the overall shape of a cycloidal mark depends only upon n, the ratio

of the Scottsbluff, Nebraska

Inidana and Ohio caused by the Palm Sunday tornadoes were not the loosened or blown-off soil from plowed fields, but they represent narrow bands in which tornup pieces of corn stubbles are piled up several inches. In fact, none of the corn fields with these marks had recently been plowed when the tornado hit on April 11. The Nebraska tornado studies by Prosser occurred on May 5 when some fields could have been plowed prior to the tornado.

It is of interest to note that Prosser feels that the marks are the result of differential soil characteristics while the author thinks that they represent narrow bands of debris accumulation. Nonetheless, both researchers seem to agree that they represent loci of spots which act like nature's vacuum cleaners. In Prosser's case, the vacuum cleaner was so strong that it loosened up and vacuum cleaned to the debris accumulation seen in the author's case can be explained as vacuum cleaners which are strong enough to converge debris, but no capable of sucking up the accumulated debris, which remains within a few-inch layer above the corn fields?

household vacuum cleaner head with 15 ft sec suction speed would produce a convergence of

Conv. = suction speed

height of head above the floor

when the head was placed about 2 inches above the floor. If we assume that a convergence of 10 sec, only one tenth of that of household vacuum cleaner, is existence near the ground, it would result in the vertical motions of 5 ft sec at 6 inches above the ground, 10 ft sec at one foot, 100 ft sec at 10 ft, etc. In order to determine the characteristics of tornadoes just above the surface, it is necessary to examine the marks in aerial pictures by means of detailed ground survey.

Despite the fact that we do not know the magnitude of the convergence giving rise to the formation of these ground marks, it is obvious that they can be produced only if the convergence near a tornado center is concentrated at several spots which rotate around the center. In case the convergence takes place uniformly around a circular area, a uniform damage belt such as produced by a rotating grinder would

present in a tornado, for example, it may be calculated that

Seil and . vi vegetation

7. The Nature of Characteristic Cycloidal Marks on the Ground

Since Van Tassel (1955) first reported on the observed elliptic marks left on fields by the North Platte Valley tornado of June 27, 1955, several other such phenomena have been reported. Prosser found a large number of cycloidal marks in a series of vertical aerial pictures photographed along the path of a Nebraska tornado of May 5, 1964. The aerial survey of the Palm Sunday tornadoes of April 11, 1965 as reported in Chapter II (SMRP Research Paper 49) revealed the existence of a large number of well-defined cycloidal marks in Indiana and Ohio.

Complete interpretations of these marks have not been made at the present time; however, both Van Tassel and Prosser concluded that they are closely related to the rotational and translational motions of each tornado. Van Tassel assumed that the marks were produced by a trapped object which rotates around the tornado of the revoluing wind within the speed of the revoluing wind within the speed of the revoluing wind within the translation. Using C, the circumference of the ellipse; N, the number of scratche rings per mile; and S, the translational speed of the tornado as input data he estimated a tangential wind speed of 484 mph based upon his closer inspection of high-resolution aerial photographs and also upon a damage survey by R. E. Meyers, State Climatologist for Nebraska who stated "the path gave the impression that an enormous vacuum cleaner had swept the ground clean of vegetation, loose soil, all other movable objects." Prosser considered, on the other hand, that these marks are probably the result of light reflected differently from the disturbed and the undisturbed areas. Careful examination of the photographs by Prosser led him to make an important suggestion that the vortex diameter was oscillating about the

In an attempt to find out the nature of these marks, the author took a number of 35-mm telephoto pictures from a low-flying Cessna-310. Figure 11, reveals the detailed structure of the marks, the overall view of which appears in Fig. 39, Chapter II. A cycloidal line super-imposed upon the telephoto picture was drawn by following smoothly one of the most pronounced lines in the picture. It will be found that there are a few more cycloidal marks within the one cycle cycloid in the figure, suggesting strongly that several "spots" rotating around the tornado center was responsible spots represent those of very strong suction capable of vacuum cleaning the soil on a plowed field, it is feasible to determine the size and position of these spots relative to the tornado center.

mean since the radius of curvature of closed loops varies along the tornado path.

Closer inspection of a number of telephoto pictures and repeated visual observation from 500 ft by the author led him to believe that the cycloidal lines in

radial outflow are plotted as functions of the radius. These intensities are defined by Vrand Vrushich can be integrated, respectively, as

 $\Gamma = \int_{0}^{2\pi} V_{t} r d\theta \qquad , \text{ circulation}$ and $F = \int_{0}^{2\pi} V_{r} r d\theta \qquad , \text{ influx,}$

where $\sqrt{\frac{1}{1}}$ and θ denote tangential velocity, radial elocity, and the horizontal angle around the cyclone axis. The quantity $\frac{1}{1}$, representing circulation or outflow per unit angle around the cyclone axis, is expressed in CGS units.

Figure 10 indicates that the circulation intensity is negative or very small distance from the in the front quadrant some 20 miles away from the center. As the center is approached decrease, the intensity gradually increases to about 100 stat mi hi rad. The intensity increase continues after the passage of the center, reaching a maximum in the rear quadrant about 15 miles from the center. We may postulate, therefore, that a certain time is required for the surface winds to acquire a cyclonic circulation when a tornado cyclone aloft moves over an area. In this specific case, about 40 min was required for the passage of the tornado cyclone.

The field of inflow intensity inside this tornado cyclone was also quite asymmetric. In the front quadrant the inflow increased to a maximum about 15 miles from the center. But the inflow intensity was more or less constant outside a circle about 8 miles in diameter. The inflow intensity around this circle was about 150 stat me hr rad. If constant convergence inside this circle is assumed, the mean convergence would be about 20 hr or about 500 x 10 sec. In the region of the tornado bounded by the dashed lines is excluded from the region of convergence by the tornado cyclone, a reduction of the convergence area would increase the convergence to about 800 x 10 sec. Nevertheless, convergence of this order of magnitude would result in a 30 to 40 ft sec updraft at the 5000-ft level.

The inflow in the rear quadrant is extremely small. This characteristic coincides with the fact that hittle or no spiral rain echoes are usually observed in the rear quadrant of tornado cyclones. Figure 3 includes two good examples of this feature; namely, April 11, 1965 and April 9, 1963 which were cases accompanied by well-developed tornado-cyclone circulations. Note that two spiral echoes with crossing angles of more than 40 are seen in both examples.

A question which will arise immediately is the diameter of such an air columne inside which the tangential speed decreases outward. According to Fig. 8, the diameter seems to be about 5 miles. About 20-mph tangential speed relative wind is seen along the outermost boundary, indicated by a dashed circle. It seems that this rotating air column, 5 miles in diameter, is acting as an obstacle to the relative winds from the east-south east. Right at the ground, where theoretically the air does not move even inside a tornado, the relative wind velocity should be opposite to that of the translational velocity of the tornado. A rotating air column such shown in Fig. 8 must, therefore, be undercut by an extremely shallow layer. As the height above the ground increases from the order of inches to feet, the relative winds quickly change into those representing a column circulation around the center of a traveling imply that the tornado inflow takes place inside a very shallow layer just above the ground.

Because of the fact that a tornado cyclone is accompanied by a much weaker wind system than that of a tornado, relative surface winds inside a tornado cyclone do not always represent a relative flow. Fig. 7 already revealed the fact that relative surface winds of a fast-moving tornado cyclone appear to blow through the region of the cyclone. Since the tornado cyclone, as well as most others, was located over a region where the southerly surface winds are about 30 mph, a moving tornado cyclone with a few-millibar pressure drop at the center is not strong enough to modify the 30 mph southerly wind or 55 mph relative wind from the east-southeast into a cyclonic flow within the area of the tornado cyclone.

Assuming, however, that a tornado cyclone induces perturbed winds, no matter how fast it travels, the field of perturbed winds can be obtained by subtracting estimated undisturbed winds from the total winds recorded by the Tecumseh wind recorder. Taking the time changes in the undisturbed wind into consideration, it was changed linearly from SSE 31 mph at 1850 CST to S 31 mph at 1925 CST. Figure 9 shows the field of perturbed wind resulting from tornado cyclone as it was moving north of Tecumseh. Adashed circle in the figure represents the region of the whirl wind around the tornado center. Winds outside the circle form a spiral flow extending to about 20 miles from the tornado-cyclone center.

It should be noted that the streamlines of perturbed winds are considerably asymmetric, suggesting that most of the inflow takes place in the front quadrant of the tornado cyclone. More quantitative aspects of such an asymmetry will be understood by refering to Fig. 10 in which the intensities of the circulation and the outside this area

wind speed toward the tornado-cyclone center, which represents the tornado center in this case. It is, therefore, difficult to depict the flow accompanying the tornado cyclone by using the relative winds as shown in Fig. 7. The whirling wind around Tornado J-4 is presented in Fig. 8 by enlarging a portion of Fig. 7. The dashed circle represents the boundary of the wind field of tornado J-4. Shown in the upper half of the dashed circle is the profile of the tangential wind speed plotted against the radii in the front and rear sectors of the storm. It shows that the tangential wind speed increases toward the center inversely proportional to the radius, implying that the eye or the core circulation of this tornado was surrounded by a irrotational,

(vr) vortex. The circulation of the vortex is estimated to be $(r = 2\pi r v \approx 180\pi m^2 hr^4)$.

If we assume that this circulation remains constant everywhere outside the core, the maximum wind at the core boundary would be

which is inversely proportional to the core radius. Tornado J-4 produced widely-scattered mobium damage to the north of the wind tower. If we assume that the 3-mile wide damage path was caused by a tornado with a core of one mile in diameter, would be about 180 mph. The maximum wind speed including the translation at motion of the storm was, therefore, about 240 mph.

In fact, fornado K-3 also contributed to the overall damage path north of Tecumseh Eyewitness accounts indicated that the first one caused most of the damage. however, Figure 1 also shows that the maximum wind speed was 85 mph which is slightly more than the translational velocity of the tornado.

6. Relative Surface Winds and Perturbed Winds Accompanied by Fast-Moving Tornadoes and Tornado Cyclones

It was shown in Figs. 7 and 8 that the wind velocity representing the vortex motion around a tornado axis near the surface can be obtained by subtracting from the total wind the translational velocity of the tornado center. In other words, the surface winds around a fast-moving tornado are very similar to those inside a rotating air column extending from near the surface upward)

progresses from A_y B_x to C. In Stage C, the central region of a tornado cyclone seems to act like a weak tornado with a very large diameter. Periodic concentration of vorticity near the central region would produce a series-mode tornadoes.

4. Circulation Around Tornado J-4 Estimated from Tecumseh Wind Records

In order to study the 151-mph gust recorded at Tecumseh, in relation to tornado J-4, a 40-min section of the wind trace in Fig. 1 was enlarged. Figure 5 shows such an enlargement including wind velocities plotted at the bottom. Using heavy line segments, the successive maxima and minima were connected to show the range of the wind fluctuation clearly. The numbers next to the plotted winds represent the gust speed in knots. The highest gust of 151 mph occured between 1907 and 1908 CST when the direction was shifting rapidly from WSW to WNW, suggesting that it was recorded when the tornado center was passing just to the north of the station.

Figure 6 was made to determine the wind field in relation to the damage area and radar hook echo "J," which produced four tornadoes of the combined mode.

The upper chart in Fig. 6 indicates that the wind tower was located near the southern boundary of the damage path. It also reveals the fact that the diameter of the eye in the PPI echo was approximately the width of the damage path. This does not mean that the diameter of the tornado eye was over two miles; it could be considerably smaller. The lower chart shows the space cross-section of winds converted from the time cross-section of the Tecumseh winds. The wind pattern seems to be affected by the cyclonic circulation of the tornado cyclone as well as by the tornado which was near the cyclone center.

Since tornado J-4 was one of the series of tornadoes belonging to a combined-mode family, we may reasonably assume that it moved with the center of the tornado cyclone at 60 mph toward the east-northeast. Due to the significantly low pressure around the tornado center, the surface wind field around the tornado axis represents a circular wind field superimposed upon a straight flow which represents the translational motion of the storm. Figure 7 shows the stream lines of relative flow and was obtained by subtracting the 60 mph straight flow from the winds recorded in Fig. 6. There are two important features in this figure. The one is that the tornado circulation appears only inside the dashed circle in the figure. The other

wind speed also decreases rapidly. Associated radar echoes would assume the shape of several spirals giving the impression that the storm is a miniature hurricane.

4. Location of Tornadoes in Relation to the Eye of the Tornado Cyclone

From the terminology point of view, if one emphasizes the geometric patterns of radar echoes, the above-mentioned four stages would represent a complete evolution of a rotating thunderstorm. If we emphasize the circulation accompanying these storms, we may consider that the circulation increases through stages A and B, reaching a maximum in stage C, and finally disappears in stage D. The whole system may thus be called a mesocyclone initiated by a rotation of a thunderstorm. According to the definition by Brooks (1949), a mesocyclone accompanied by one or more tornadoes is called a tornado cyclone.

Surveys of tornadoes indicate that a family of tornadoes forming inside a tornado cyclone may form in one of three modes: the parallel mode, the combined mode, and the series mode. Based on the damage surveys of the Scottsbluff tornadoes by Van Tassel (1955), the Fargo tornadoes by Fujita (1960), the Dallas tornadoes by Hoecker (1958), the Worcester tornadoes by Penn et al. (1955), the Blackwell tornadoes by Staats and Turrentine (1956), the Illinois Tornadoes by Fujita (1958), and Chapter II (SMRP Report No. 49), the positions of the tornadoes relative to the tornado-cyclone center are shown in Fig. 4. In this model of tornado paths, formation of parallel-mode tornadoes takes place mostly on the right side of the eye of a tornado cyclone, While those of the series mode occur near the center of the eye. Of interest is the change the parallel mode to the series mode. Such a change has been found quite frequently. However, no case in which a series-mode family changed into a parallel-mode family has been found. This would imply that the structure of a tornado cyclone, which is favorable for the production of a parallelmode family, somehow changes into that likely to produce a series mode. Further study has indicated that the parallel-mode family forms out of storms in Stage B, the Development Stage, while the series-mode one forms out of storms in Stage C, the Mature Stage. The reason for such a preference in tornado families is not known at the present time. We may suspect, however, that the concentration of vorticity around the center of a tornado cyclone takes place as the storm stage

which stands semi-vertically and is surrounded by a vortex of high tangential velocity. Fujita (1958) estimated that the tangential velocity around the eye of the storm which produced the Illinois tornadoes of April 9, 1953 was about 40 kt at a distance of one mile from the center of the eye. A collection of four heek-echo radar pictures of hook-echo appears in Fig. 3. Three examples suggest that the vault is predominant in very early stage of the hook-echo development when the rotational rate of a thunderstorm claude. is relatively low. As the rotation becomes faster, an eye forms to the south or southeast end of the vault. Even though we have not obtained a good example of a radar picture showing a well-developed vortex around the eye, it would be natural to suspect that such a picture would appear as a miniature hurricane with several spiral echo bands surrounding an eye.

The evolution of a hook-echo circulation may be expressed as follows:

- A. <u>Initial Stage</u>: A thunderstorm starts rotating slowly, forming a vault in the region where the updraft is the strongest. According to Browning's (1964) definition a vault may appear even before the onset of the storm's rotation as long as the updraft is sufficiently intense to result in inadequate time for droplet growth and is inhibiting the reentry of large hydrometeors.
- B. Development Stage: As the storm's rotational rate increases, the air converging toward the foot of the updraft canno longer reach the circulation center because of the large angular momentum, that must be transported inward without increasing the tangential velocity enormously, is too large. Thus a small eye forms at the low level first and rapidly extends upward.
- C. Mature Stage: In this stage, the eye of the storm reaches almost to the top of the cloud, thus initiating upper divergence or significant outflow at the cloud-top level. Such a divergence aloft would efficiently inhibit the entry of hydrometeors into the eye from the cloud-top level. Near the ground, an intense inflow with strong tangential velocity creates a vertical column of rotating air surrounding the eye. The tangential velocity outside the circle of maximum wind would drop hyperbolically outward. The diameter of noticiable circulation will be about 30 miles.
- D. <u>Dissipating Stage</u>: The diameter of the circulation reaches a maximum in this stage. The diameter then decreases as the maximum tangential

2. Recorded Traces of Tornado and Tornado Cyclone Winds

Despite the fact that the Palm Sunday tornadoes of April 11, 1965 left more than 30 damage paths over a six-state area, only one anemometer was near enough to a path to record tornado-related winds. This one was located at Meyers Airport, north of Tecumseh, Michigan and was operated by the Tecumseh Community Health Study, the University of Michigan. As indicated in aerial survey map No. 11 in Chapter II (Figure 13, SMRP Research Paper No. 49), the wind tower was located along the southern boundary of a very wide damage path resulting from tornado J-4. The anemometer recorded a peak gust of 151 mph at 1907 CST. About one hour later another tornado, K-3, passed north of the same anemometer, recording a 75 mph peak gust at 2004 CST. The gust recorder trace converted into rectangular coordinates with wind direction added is shown in Fig. 1. It is seen that the wind speed increased from about 30 mph to 151 mph in about 15 min, then dropped back to 30 mph in three to four minutes. After the passage of the first tornado, 1-43, the wind direction returned to southerly and remained there until about 10 min before the arrival of the second storm (K-3). The latter was located just ahead of the cold front, referred to as a dry, cold front in previous chapters. Note that a straight westerly wind with a gust up to 70 mph came shortly after this storm.

According to the analysis of the radar echoes as presented in Figs. 17 and 18 in Chapter V (SMRP Research Report No. 51) these two tornadoes were born from two separate thunderstorms which traveled along almost identical paths. A reduced gain picture of these thunderstorms taken by the Detroit (DTW) WSR-57 radar at 1852 CST appears in Fig. 2. Both echoes show distinct hooks with a cyclonic finger located in the southwest guadrant.

3. Formation of Vault and Eye in a Rotating Thunderstorm

It has been well documented that tornadoes appear in the vicinity of a hook echo characterized by a well-defined finger or a 6-shaped configuration observed in the southwest quadrant of a thunderstorm echo obtained by low-level, reduced-gain PPI scans. In Browning's and Fujita's (1965) comments and reply on the difference between the "vault" and the "eye", Fujita suggested that the eye should be clearly distinguished from the vault since the former represents a small, circular column

- ¹ The research presented in this paper has been sponsored by the U.S. Environmental Science Services Administration under grant No. E-86-67-(G).
- ² A comprehensive study of the Palm Sunday tornadoes of April 11, 1965 was originally planned to include the following seven chapters:
 - Chapter I Locations and Times of Tornadoes,
 - Chapter II Aerial Survey of the Palm Sunday Tornadoes. SMRP Rep. No. 49,
 - Chapter III The Synoptic Situation,
 - Chapter IV Early Stage of Tornado Development as Revealed by Satellite Photographs. SMRP Rep. No. 50,
 - Chapter V.- Features and Motions of Radar Echoes. SMRP Rep. No. 51,
 - Chapter VI Stability and Differential Advection Associated with Tornado Development. SMRP Rep. No. 52,
 - Chapter VII Estimated Wind Speeds of the Palm Sunday Tornadoes. SMRP Rep. No. 53.

Chapter VII concludes the portion to be submitted by SMRP.

Further plans for the completion and publication of the comprehensive study are being considered.



ABSTRACT

The wind speed of a tornado in relation to its parent tornado cyclone is discussed in this last chapter² on the Palm Sunday tornadoes. One of the most interesting wind traces in this study, obtained from Tecumseh, Michigan, showed a peak gust speed of 151 mph, at which time the recorder pen went off the scale. The radial distribution of gust speeds around the tornado indicated that the outer vortex of the tornado was characterized by an irrotational wind filed in which the product of and r is constant. An indirect wind-speed estimate was attempted by examining the characteristic cycliodal mark is left on the fields along the tornado paths. These marks are assumed to be produced by several spots rotating with the tornado funnel. Microscale convergence effects beneather these spots are estimated to be much larger than in other parts of the funnel, so that streaks of disturbed features remain along the cycloidal paths of these spots. The computed tangential speed of the spots is slightly higher than 100 mph inside the tornado paths of moderate damage.

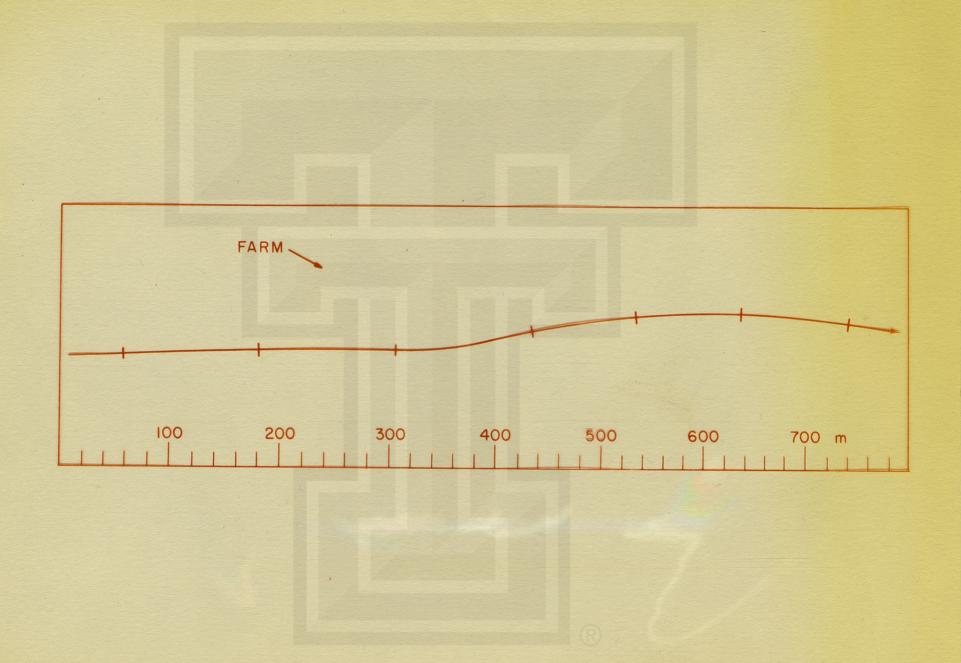
1. Introduction

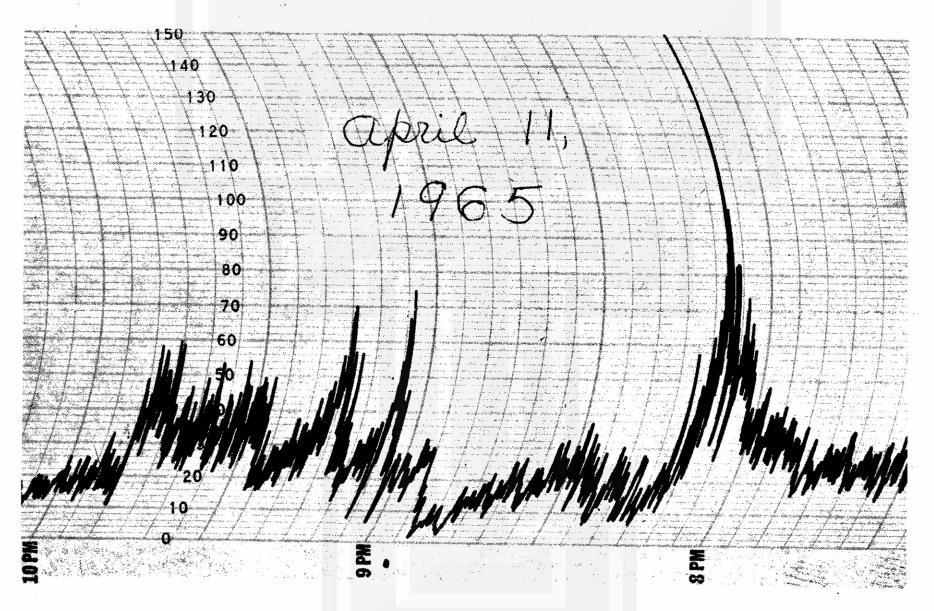
The Palm Sunday tornadoes had many remarkable features. Due to the rapid motion of the parent thunderstorms, most of the tornadoes traveled atta rate in excess of 60 mph. One by one, as many as six the number of tornadoes were systematically born out of the parent thunderstorms as described in Chapter V (SMRP Research Paper No. 51). Moreover, a rare event occurred when one of the tornadoes passed a short distance from a wind recorder which indicated a 151 mph gust. Since most of these tornadoes occurred within a few hundred miles of Chicago, an easy flying distance, a large number of aerial photographs were obtained for the purpose of examining the damage areas which might include features related to the speed of the tornadic winds.

Even though this study does not conclusively establish the wind speed of tornadoes, the discussion presented will stimulate interest on tornado winds among those who wish to investigate the nature of the most violent vortex in the atmosphere.

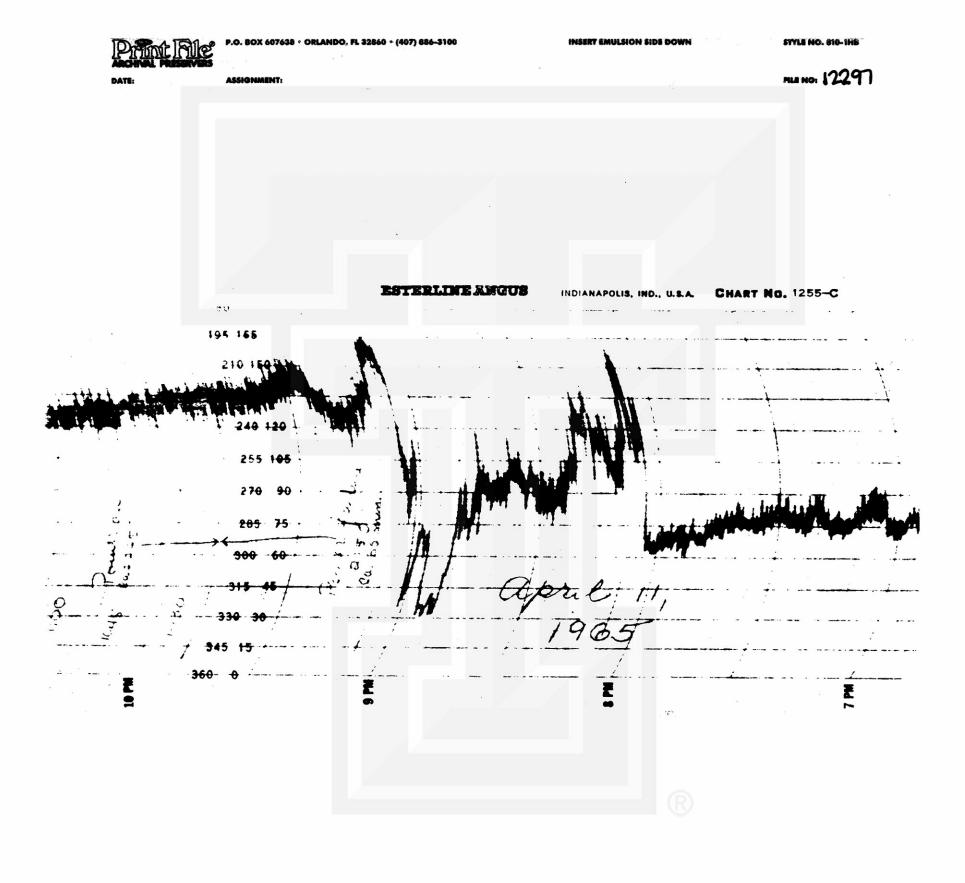
- Fig. 7. This shows that an area within a circle of 5 mi in diameter was characterized by a tangential wind speed inversely proportional to the radius. The expected region of the eye of the tornado is indicated by the fine dashed line.
- Fig. 9. Perturbed wind field accompanied by the tornado cyclone in Fig. 1. Note that this wind field shows a definite sign of circulation and convergence, since this part of the wind field represents the vector difference between the actual wind and the undisturbed wind, computed by assuming that there was no tornado cyclone.
- Fig. 10. Radial distribution of circulation intensity inside the front and rear quadrant of the tornado cyclone. These intensities were computed from the perturbed winds as a function of the distance from the storm center.
- Fig. 11. An aerial photograph of typical suction and drift marks left by a tornado on an unplowed field. This picture was taken with a 135-mm telephoto lens while flying over the area shown in Fig. 13, Chapter II (SMRP Research Paper No. 49).
- Fig. 12. Theoretical cycloidal suction marks obtained by increasing the ratio of tangential velocity, V, to translational velocity, U, from 1.0 to 10.0. Note that the size of the loops increases as the tangential speed increases.
- Fig. 13. Variation of n, the ratio between tangential and translational speeds, and S, the relative shift, as functions of relative loop width, W, which can be measured on a rectified aerial photograph showing suction marks. This figure is used in determining both n and S from aerial photographs.
- Fig. 14. An x-t diagram showing the time and locations of Family L tornadoes in Indiana and Ohio. Refer to Fig. 2, Chapter II (SMRP Research Paper No. 49), for a more detailed picture.
- Fig. 15. A rectified aerial photograph showing a large number of cycloidal suction marks. Refer to Fig. 39, Chapter II (SMRP Research Paper No. 49) for the original photograph.
- Fig. 16. Change in the shape of the tornado core as determined from the analysis of the cycloidal suction marks shown in Fig. 15 (lower part). Core diameter, rotation periods, and funnel positions 1 through 7 are given in the upper part. It should be noted that the rotational rate increased as the core diameter decreased, suggesting a conservation of angular momentum.

- Fig. 1. Wind recorder trace from Tecumseh, Michigan, on 11 April 1965, when two tornadoes passed north of the station. The recorder pen went off the chart at 151 mph. A combination of wind direction and wind speed indicates that the peak gusts at 1908 and 2004 CST were caused by two tornadoes, and the one at 2014 CST by straight winds associated with the passage of the cold front. (Courtesy of the Tecumseh Community Health Study, the University of Michigan).
- Fig. 2. A WSR-57 radar picture from Detroit taken at 1852 CST with the cold front superimposed. Comparison of this picture with Fig. 1 shows the relationship between the peak gusts and the weather systems which produced them.
- Fig. 3. Four radar pictures showing stages in the intensification of tornado-cyclone circulation. Note that the first picture, a tornadic storm south of Chicago on 22 July 1963, shows a pendant finger attached to a large echo to the north. The circulation intensity appears to increase from picture 2 through picture 4 which represent the northeast Kansas tornadoes of 19 May 1960, the Palm Sunday tornadoes of 11 April 1965, and the Illinois tornadoes of 9 April 1953, respectively.
- Fig. 4. Three modes of damage paths produced by a family of tornadoes, namely; parallel, combined, and series modes.
- Fig. 5. Enlargement of the wind recorder trace appearing in Fig. 1. In completing the wind speed chart, both time and speed of all visible maximum and minimum values were read from the recorded trace and then connected with straight lines. At the same time, successive maximum and minimum values were separately joined to show the range in the variation of gusty winds. Wind velocities plotted at the bottom represent 1-min means of maximum values in mph.
- Fig. 6. Damage area in relation to the hook echo at the time of the highest recorded wind (upper chart), and to the space section of the mean maximum winds (lower chart).
- Fig. 7. The space section of relative winds obtained by subtracting 60 mph, the translational velocity of the storm, from the 1-min means of maximum winds. Due to the rapid motion of the tornado cyclone, the relative winds computed tend to blow through the tornado cyclone near the ground. Inside the tornado area, as indicated by the dashed circle, the relative winds are circulating around the tornado center.
- Fig. 8. Enlargement of the field of relative winds inside the dashed circle shown in



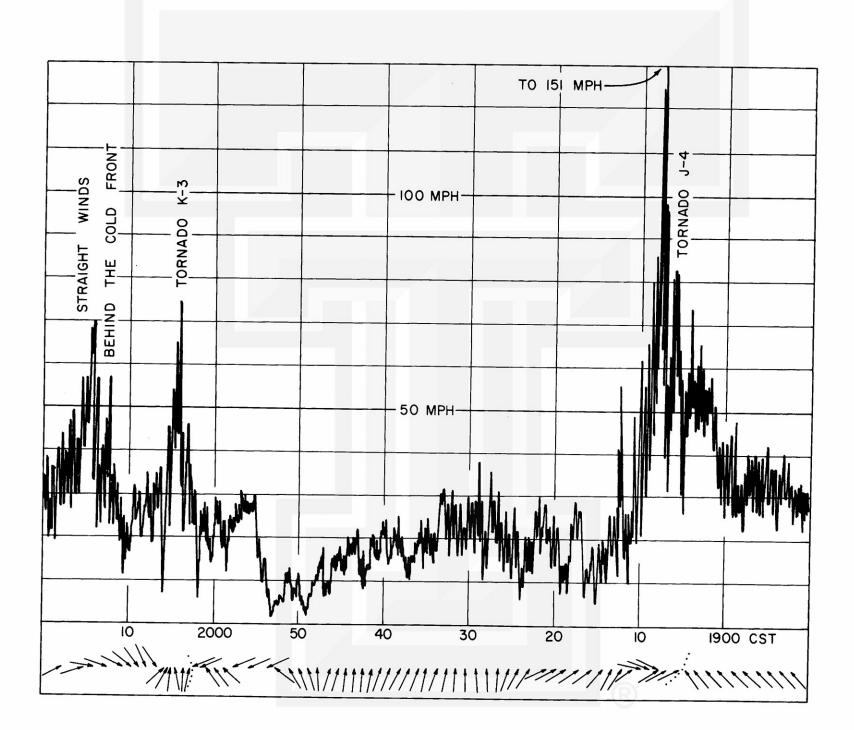


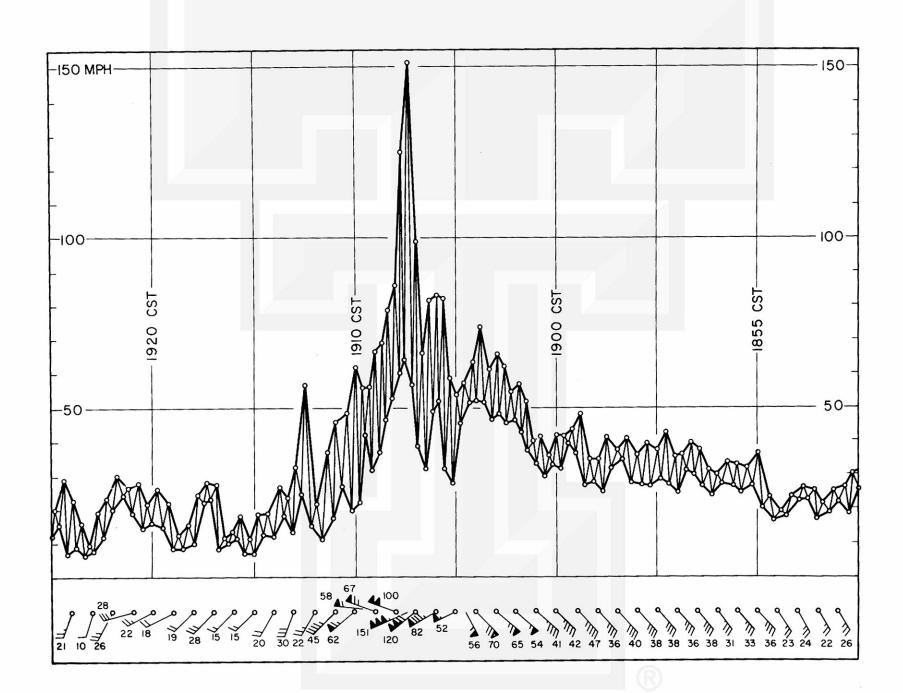
The wind blew at 150 miles per hour – and probably then some! This is the graph taken from the Community Health Study anemometer at Meyers Airport. It shows a top-of-the-scale reading at 8 p.m. and 75 miles per hour an hour later.



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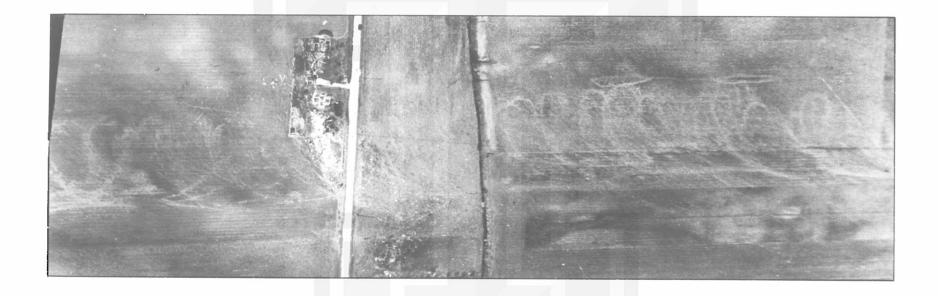
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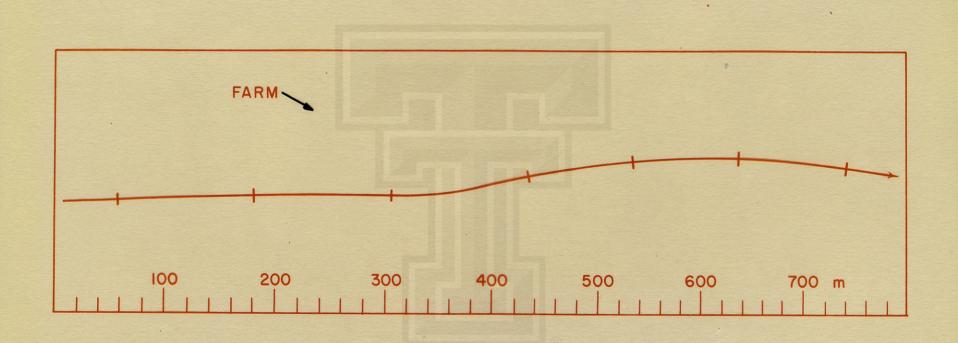
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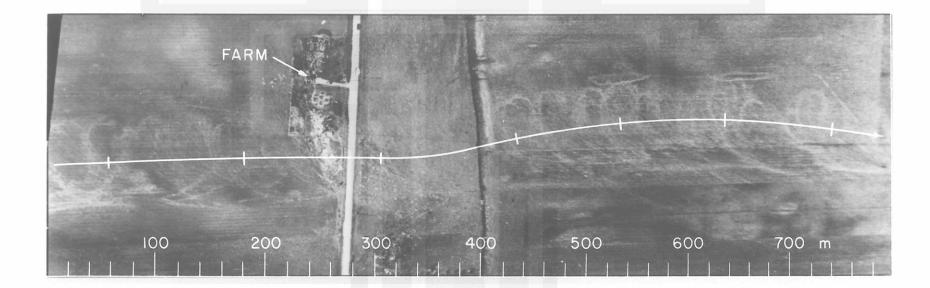


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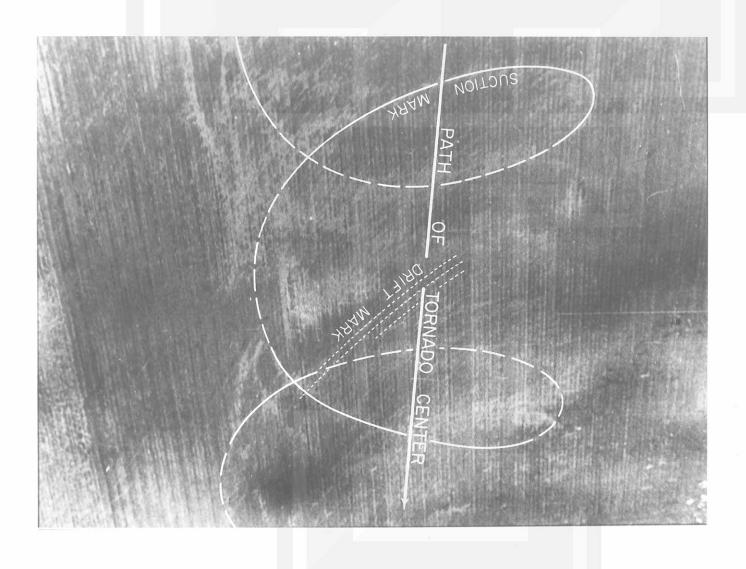
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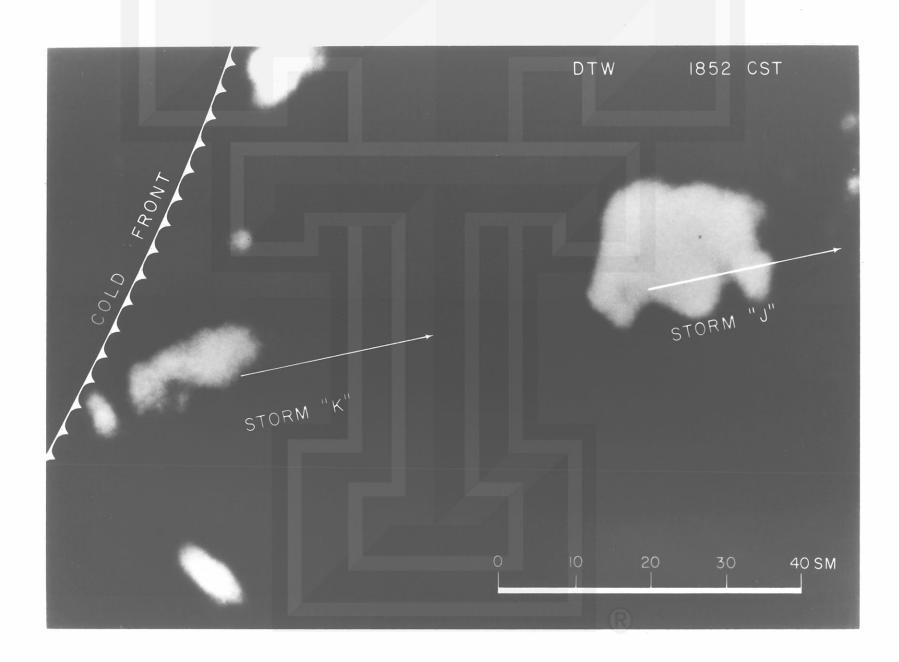
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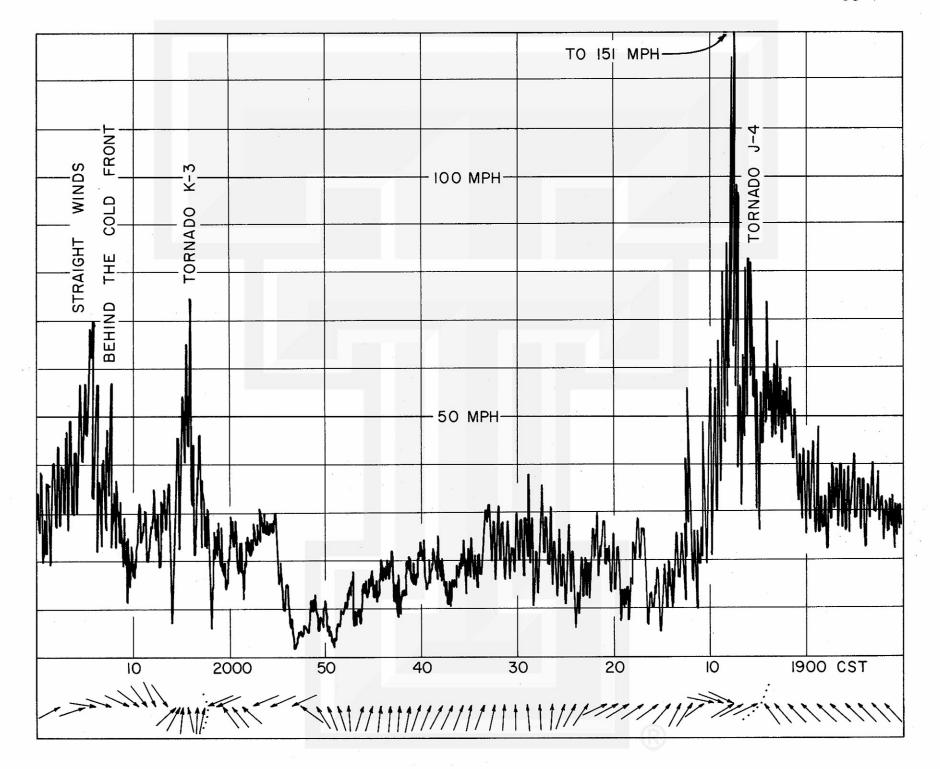


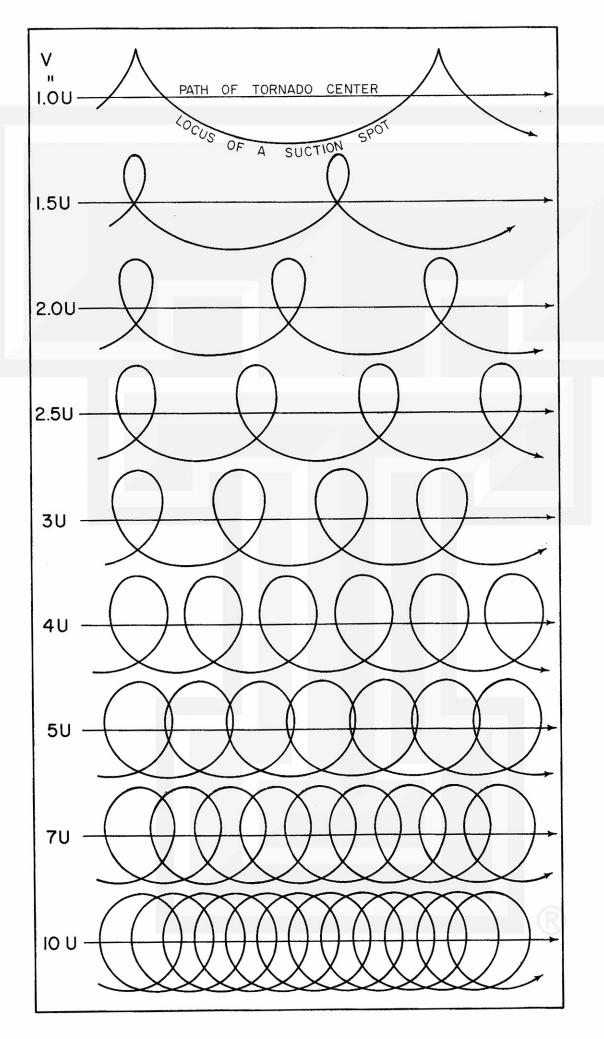


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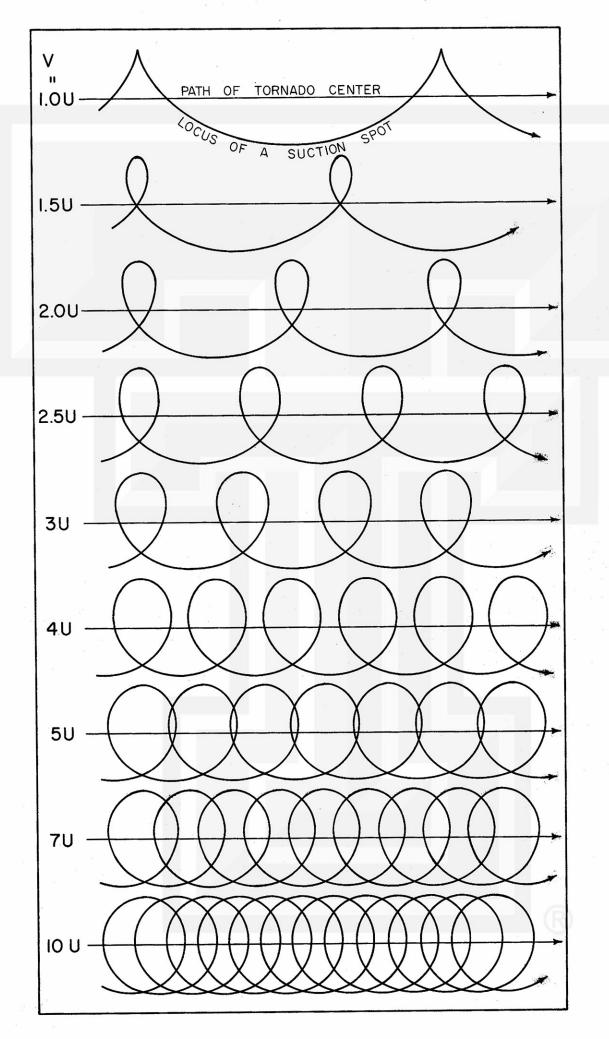


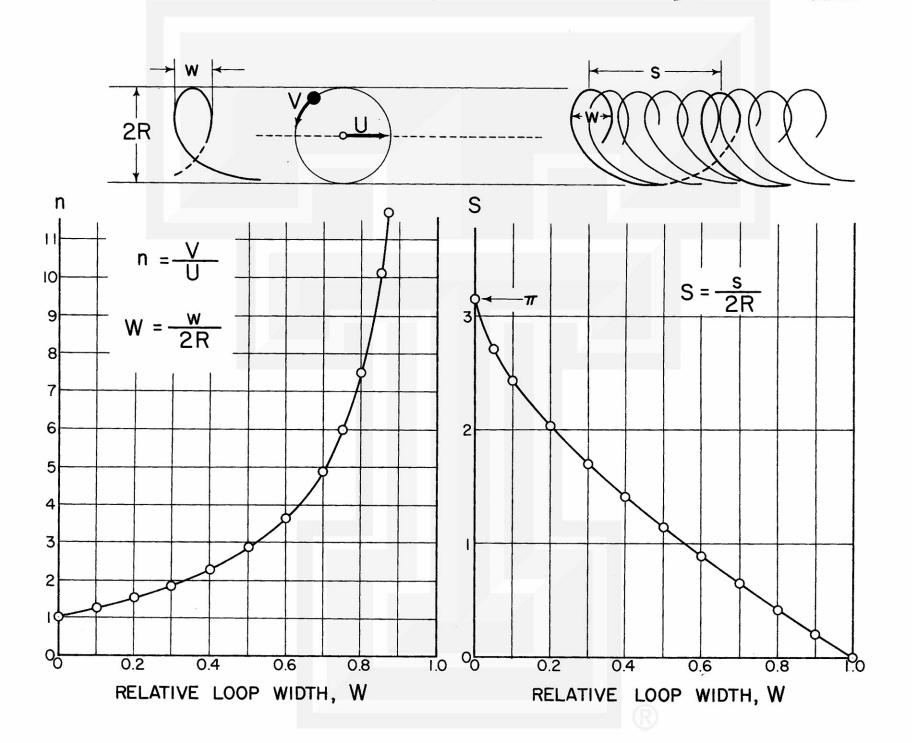


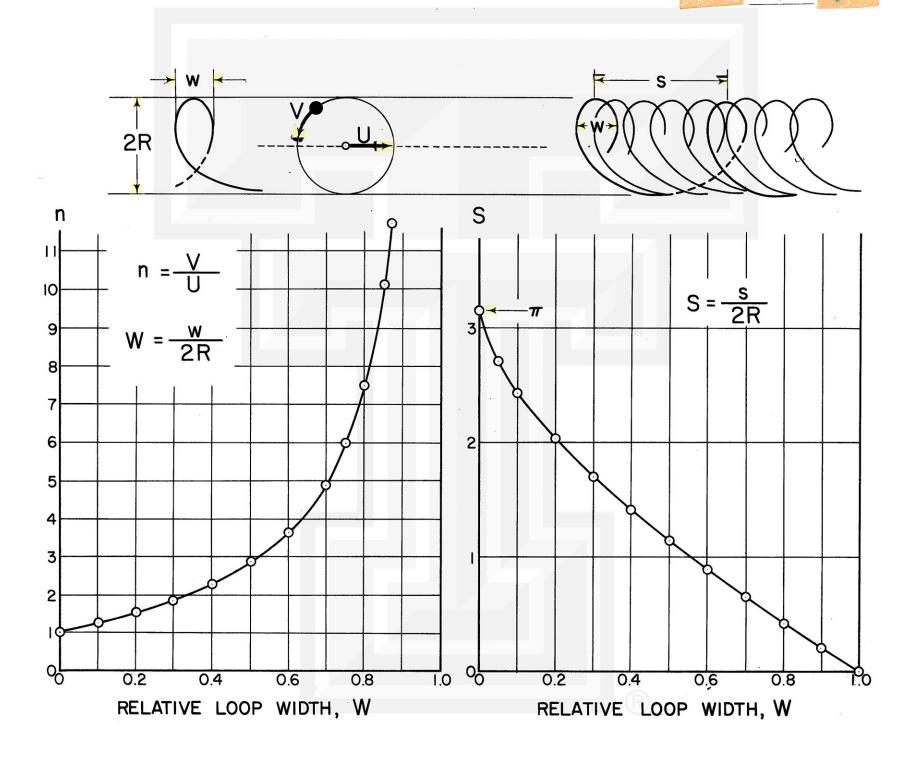


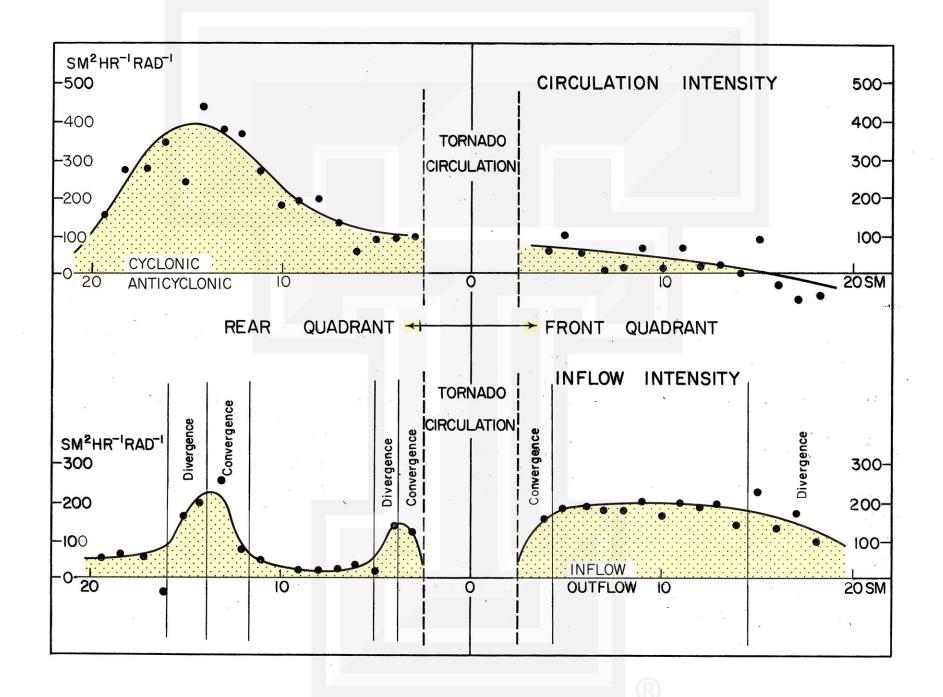
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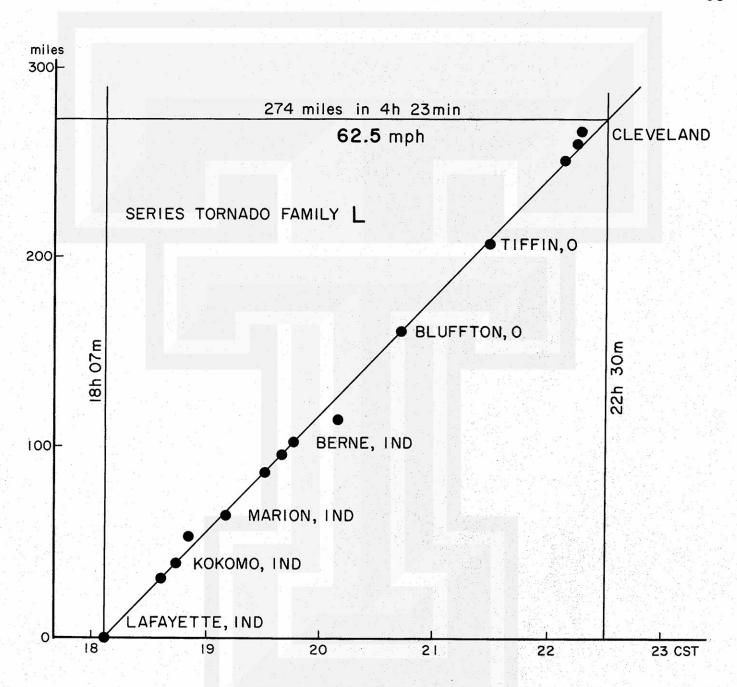
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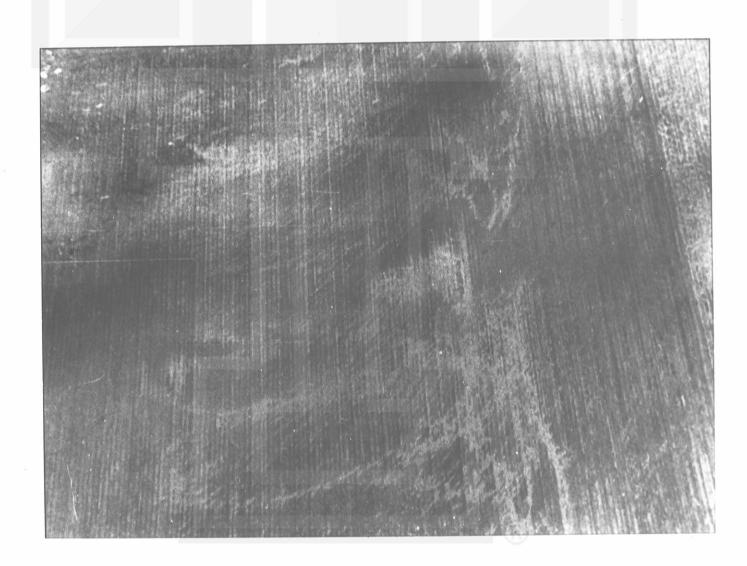
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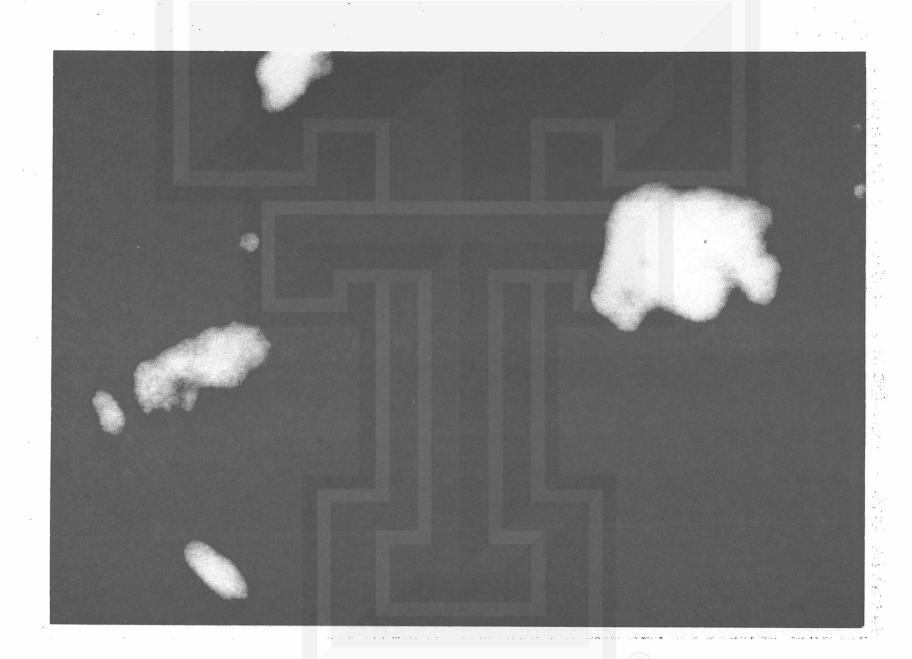
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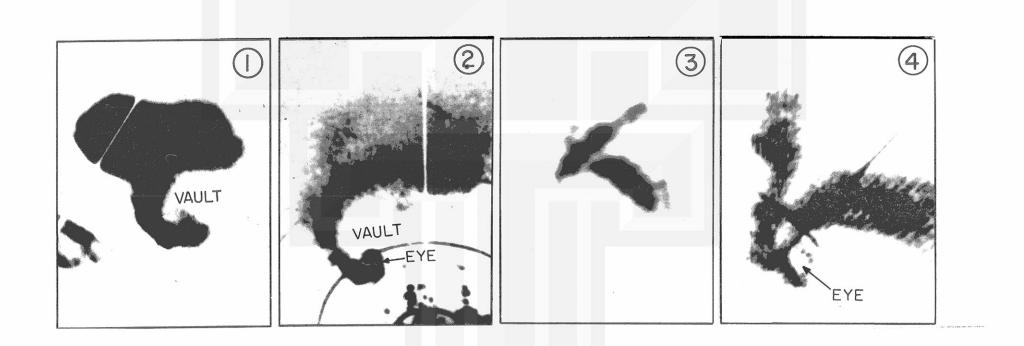












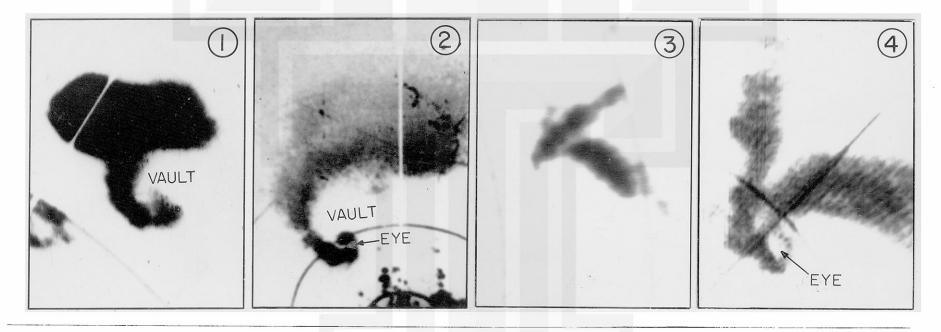
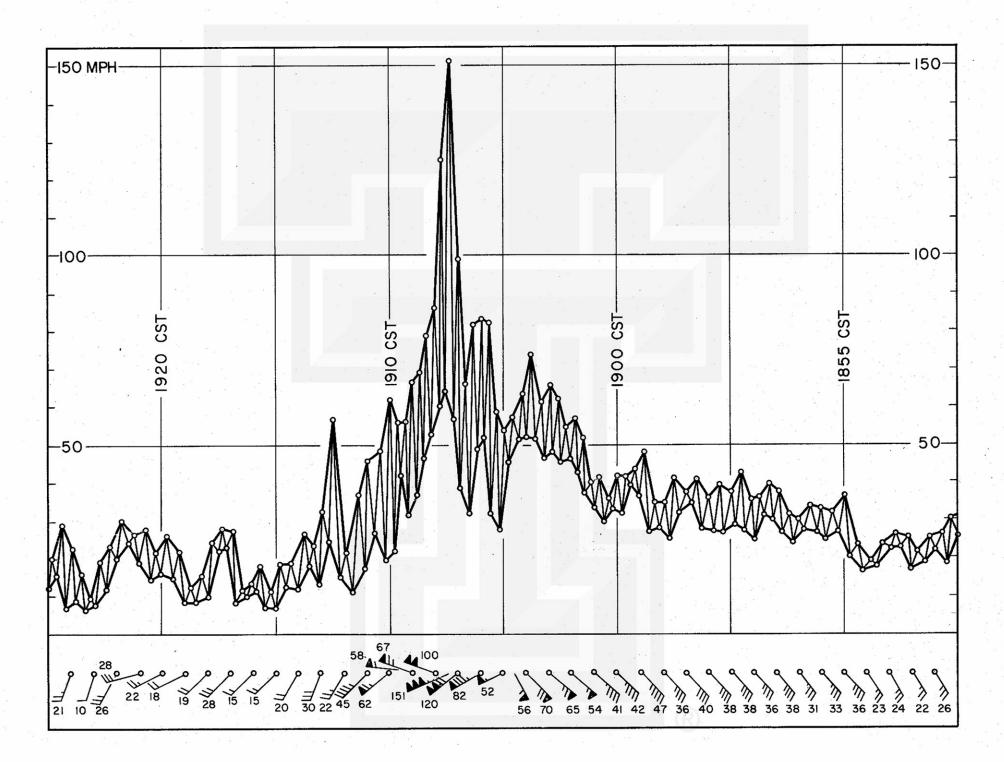
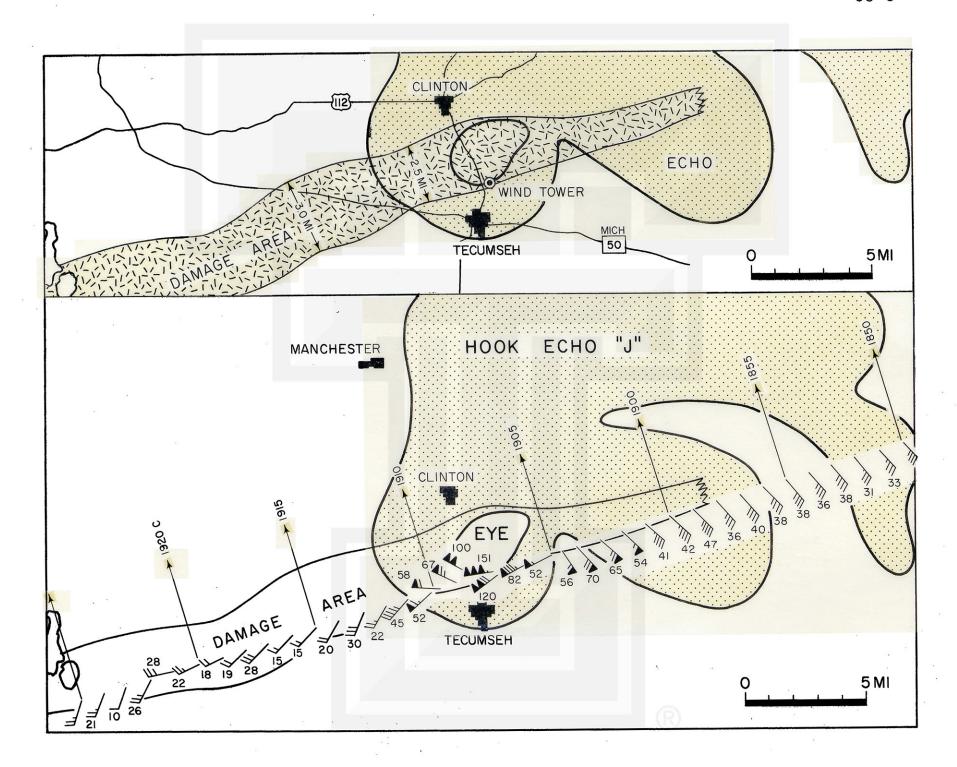
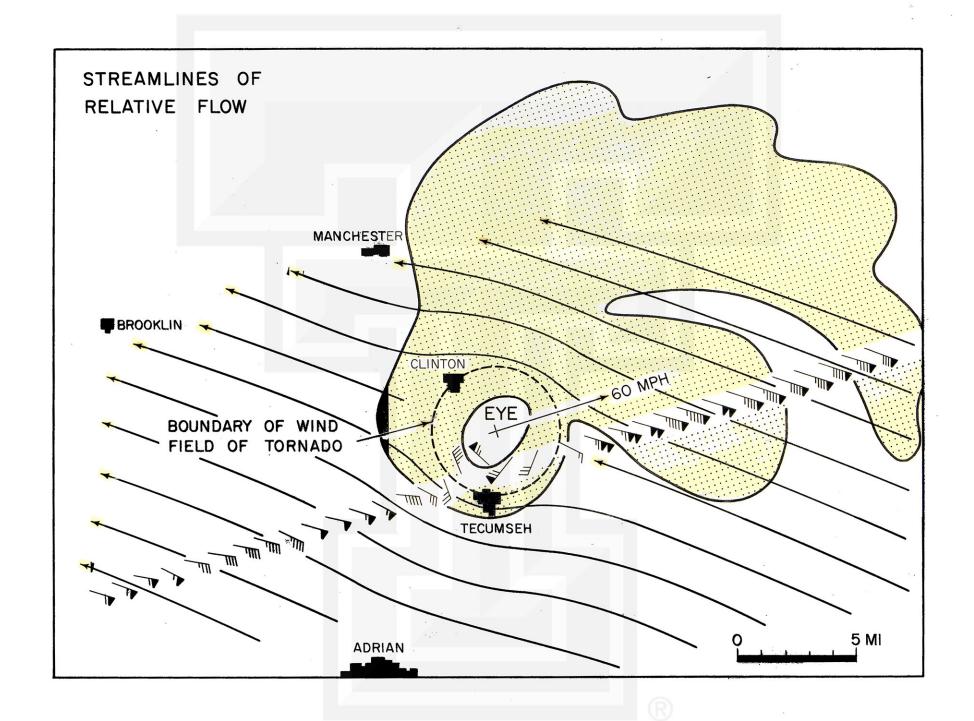
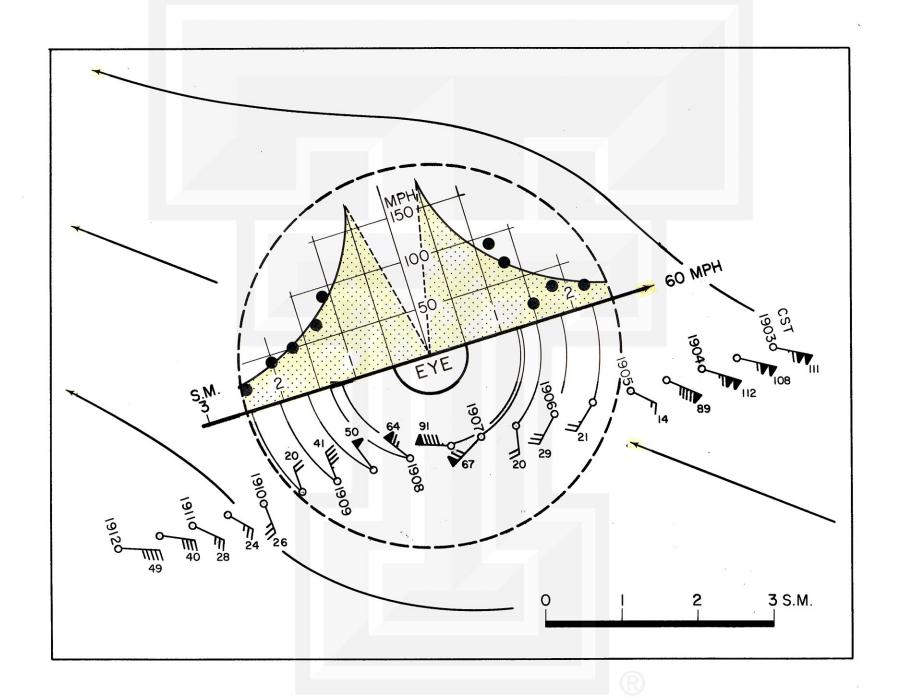


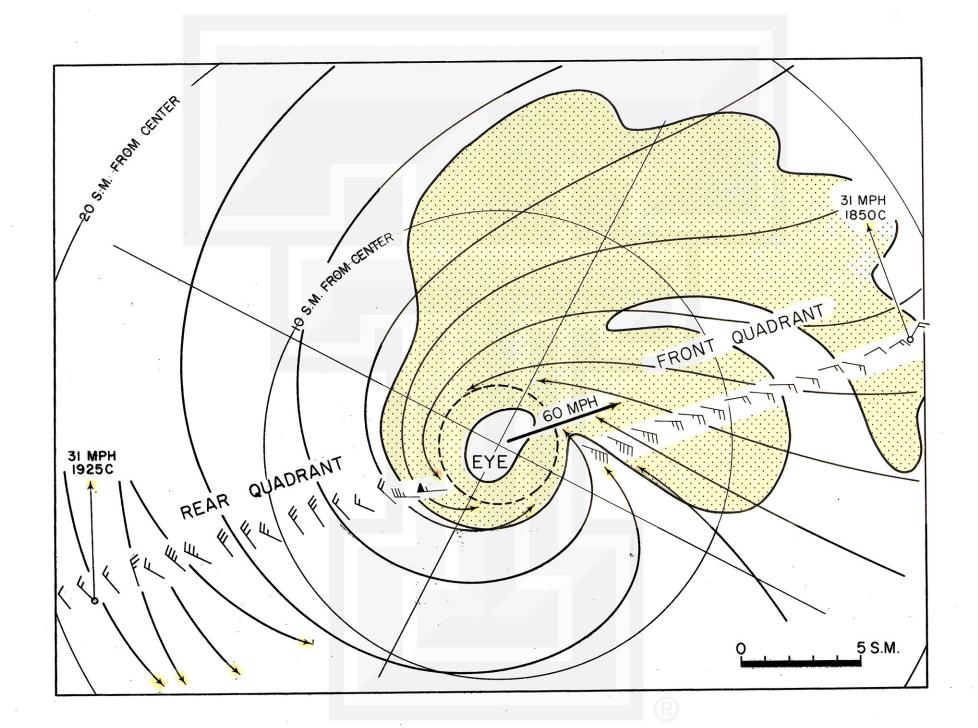
Figure 2a. Examples of echoes with rotational characteristics accompanied by tornadoes. 1. Tornadic Storm south of Chicago, July 22, 1963. 2. Northeast Kansas tornadoes of May 19, 1960. 3. Palm Sunday Indiana tornadoes of April 11, 1965. 4. Illinois tornado of April 9, 1963.

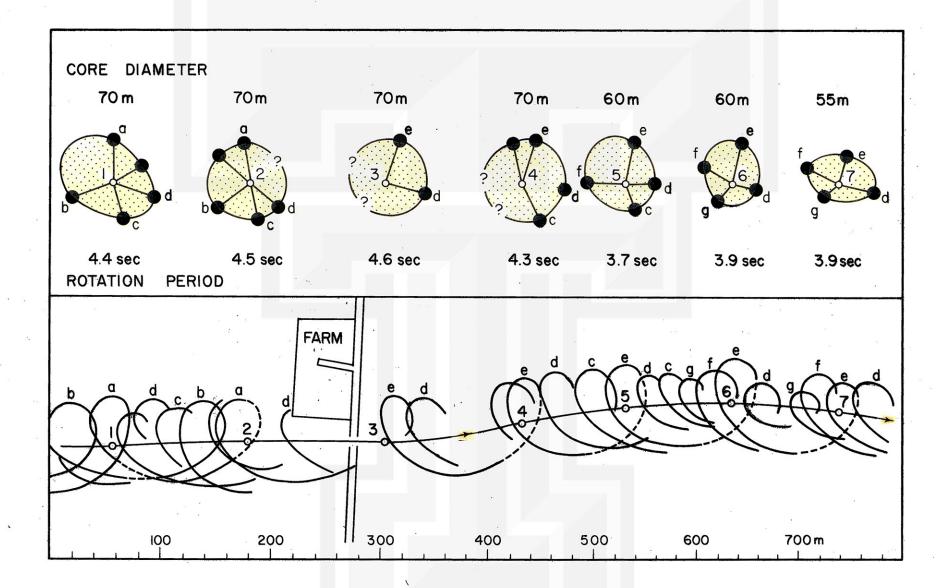












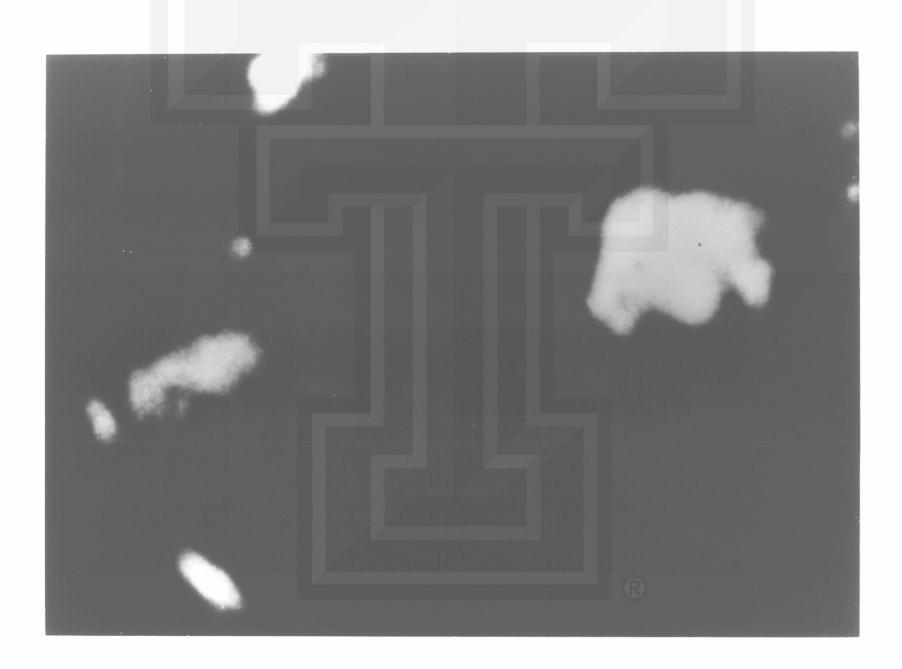
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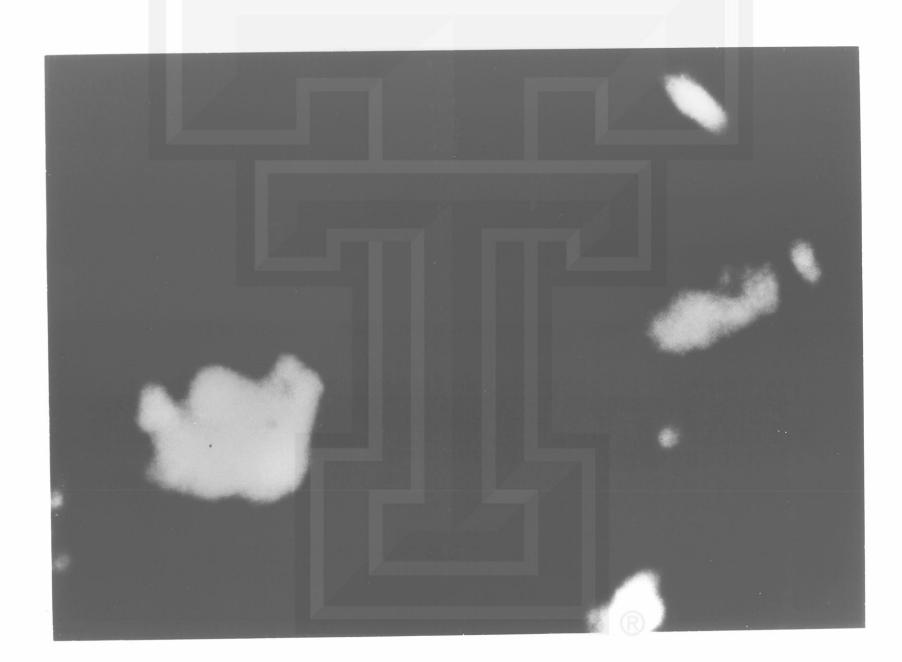


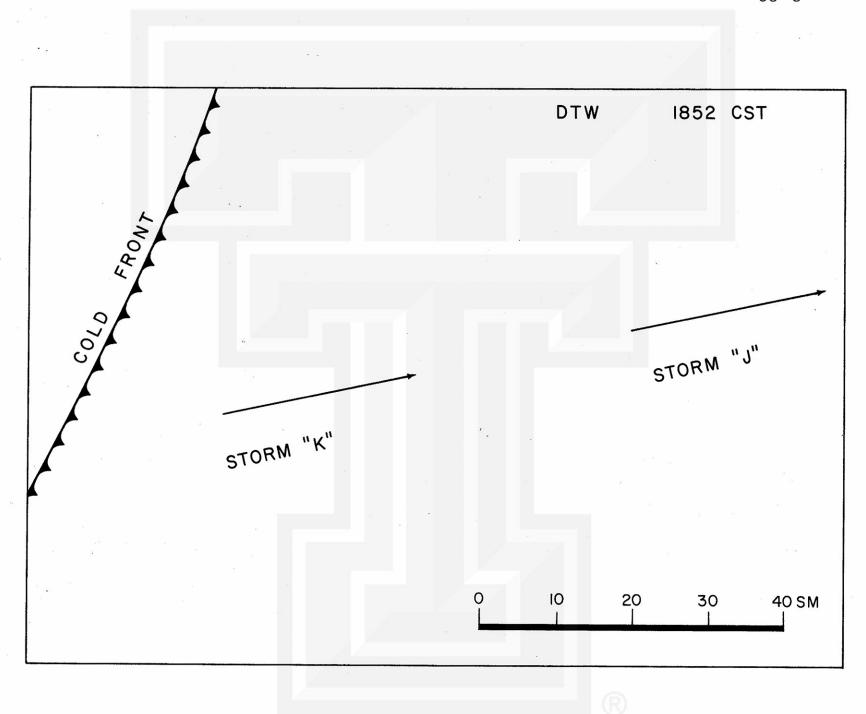


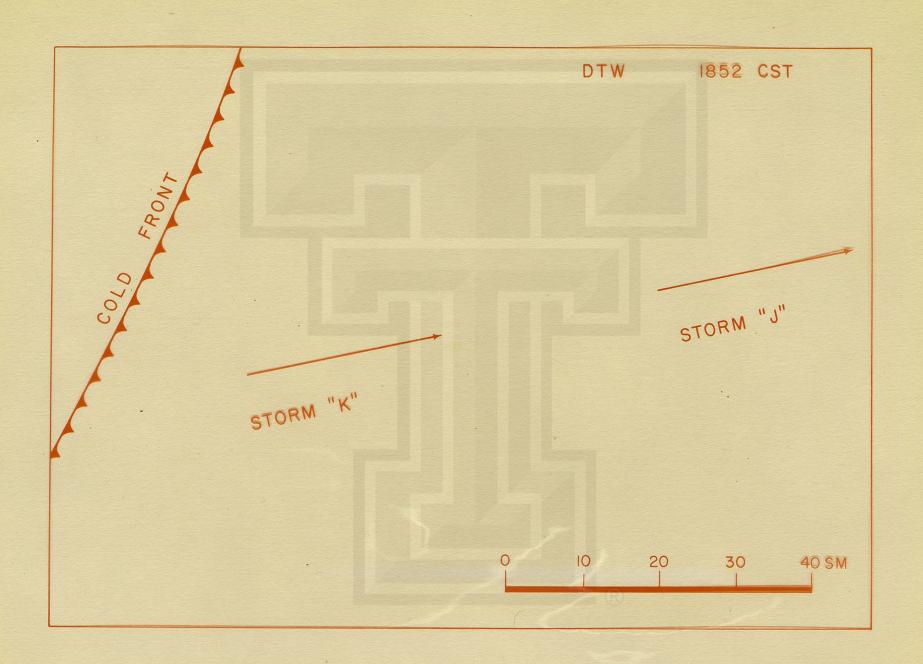
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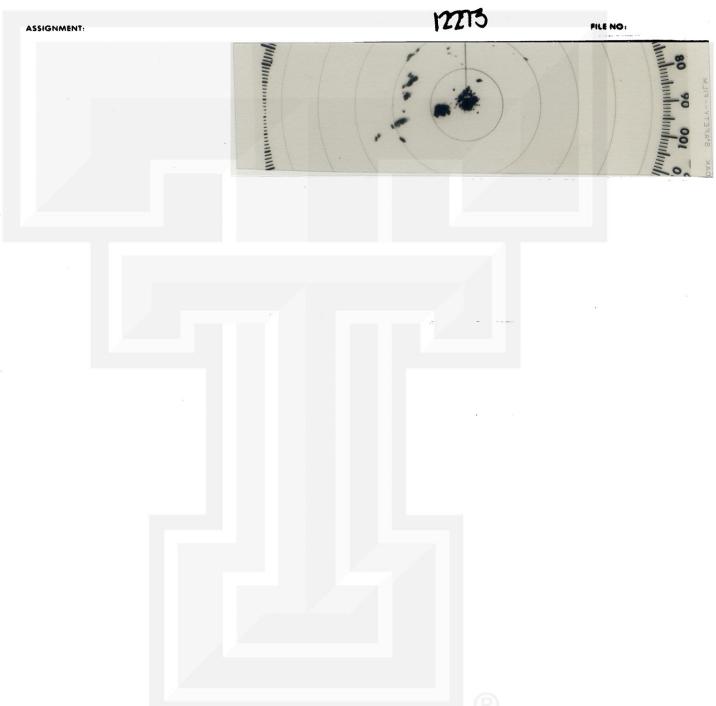
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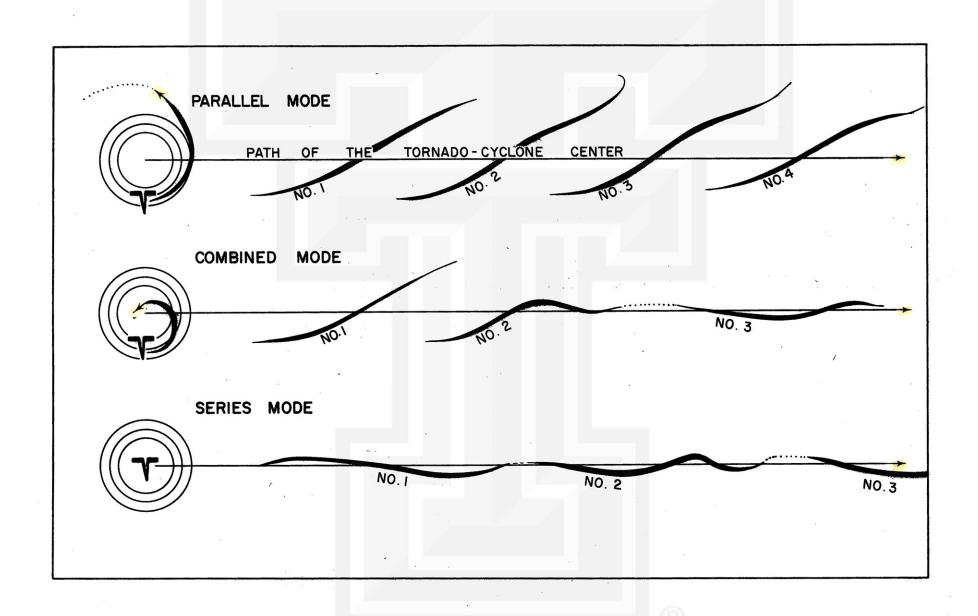






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